



UNIVERSITY OF SCIENCE AND TECHNOLOGY OF CHINA

Simulation of Resistive Instabilities in the presence of Runaway Current



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Outline

◆ Motivation

◆ Physical Model

◆ Simulation Results

➤ Linear results

➤ Nonlinear results

◆ Conclusion and discussion

Motivation

◆ During the disruption:

➤ Damage of runaway electrons to the first wall

➤ During the thermal quench, temperature drops quickly, resistivity increases correspondingly, plasma current starts to decay.

➤ During the current quench, the current is contributed partly or completely by runaway current.

➤ Runaway current profile is usually more peaked than the pre-disruption current, may induce resistive instabilities.

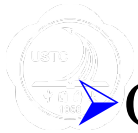
➤ Resistive instabilities may influence the confinement of runaway electrons.



Motivation

- ◆ The generation of runaway current (H. Smith, *et.al.*, *PoP*, 2006)
- Two of the generation mechanisms: Dreicer and Avalanche

$$\frac{\partial n_{re}}{\partial t} = \frac{\partial n_{re}^I}{\partial t} + \frac{\partial n_{re}^{II}}{\partial t}, \quad (1)$$



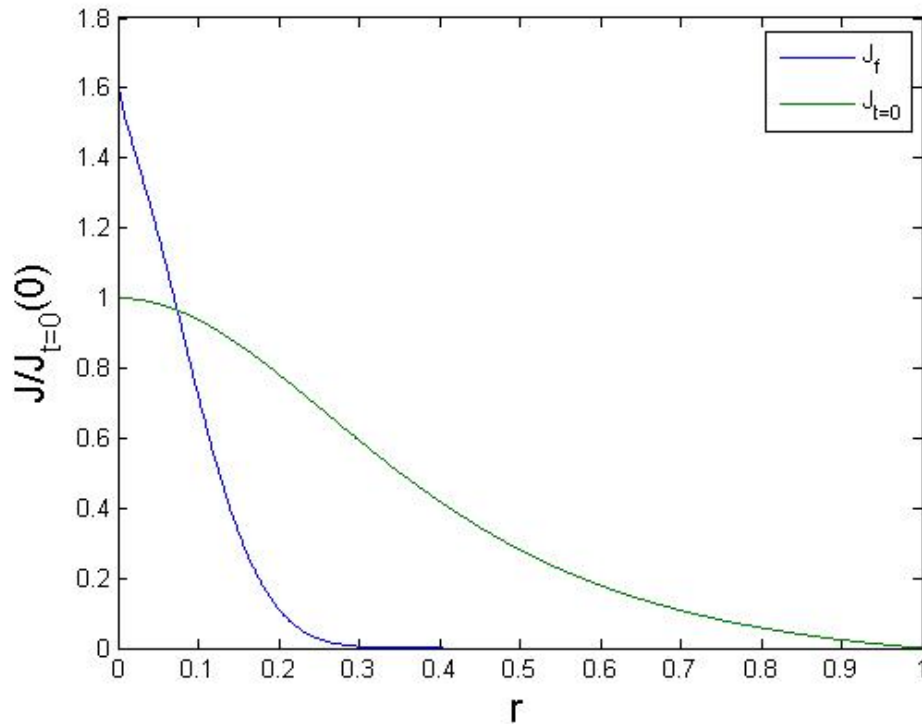
➤ Ohm's Law and Faraday's Law

$$J_{||} = \sigma_{||} E_{||} + en_{re}c, \quad (2)$$

$$\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial E_{||}}{\partial r} \right) = \mu_0 \frac{\partial J_{||}}{\partial t}, \quad (3)$$

Motivation

◆ The initial and final current profile



calculated from the above model

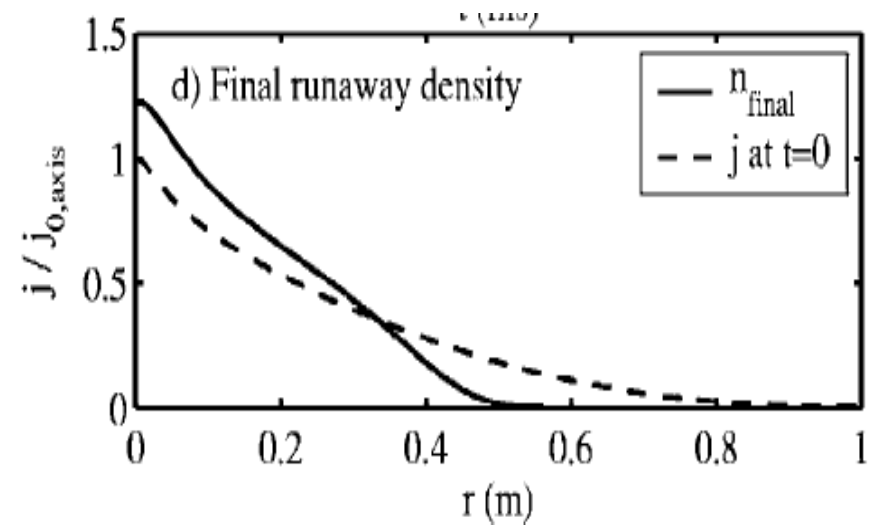


FIG. 2. A simulation of the runaway dynamics in JET discharge 63 133.

H. Smith, *et.al.*, *PoP*, 2006

Physical Model

◆ Parallel Ohm's Law

$$E_{||} = \eta(J_{||} - J_{re}) \quad (4)$$

◆ Momentum equation

$$\rho \frac{d\mathbf{v}}{dt} = -\nabla p_c - \nabla \cdot \mathbf{P}_{re} + \mathbf{J} \times \mathbf{B} \quad (5)$$

◆ Runaway density equation

$$\frac{\partial n_{re}}{\partial t} + \nabla \cdot \left(n_{re} v_{||} \mathbf{b} - n_{re} \frac{m_e v_{||}^2}{eB} \mathbf{b} \times \boldsymbol{\kappa} - n_{re} \frac{\mathbf{b} \times \mathbf{E}}{B} \right) = 0 \quad (6)$$

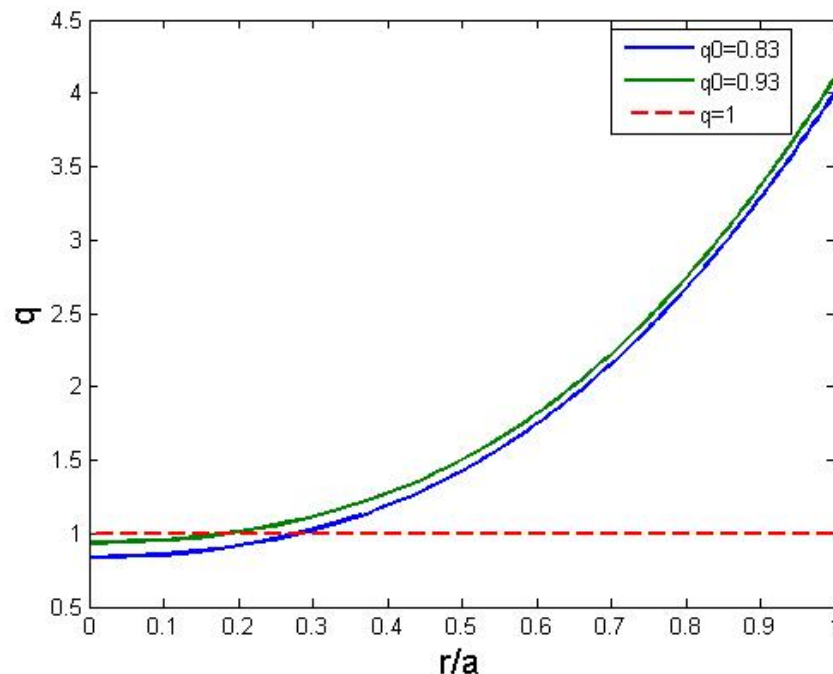
$J_{re} = -en_{re}v_{||}$, $P_{re} = n_{re}m_e v_{||}^2$, $|v_{||}| \sim c$ is assumed. Due to this assumption,

Eq.(6) is derived from the drift kinetic equation, similar to that of Helander,et. al., PoP, 2007

◆ Implement the above extended-MHD model in the M3D-k code.

Simulation results

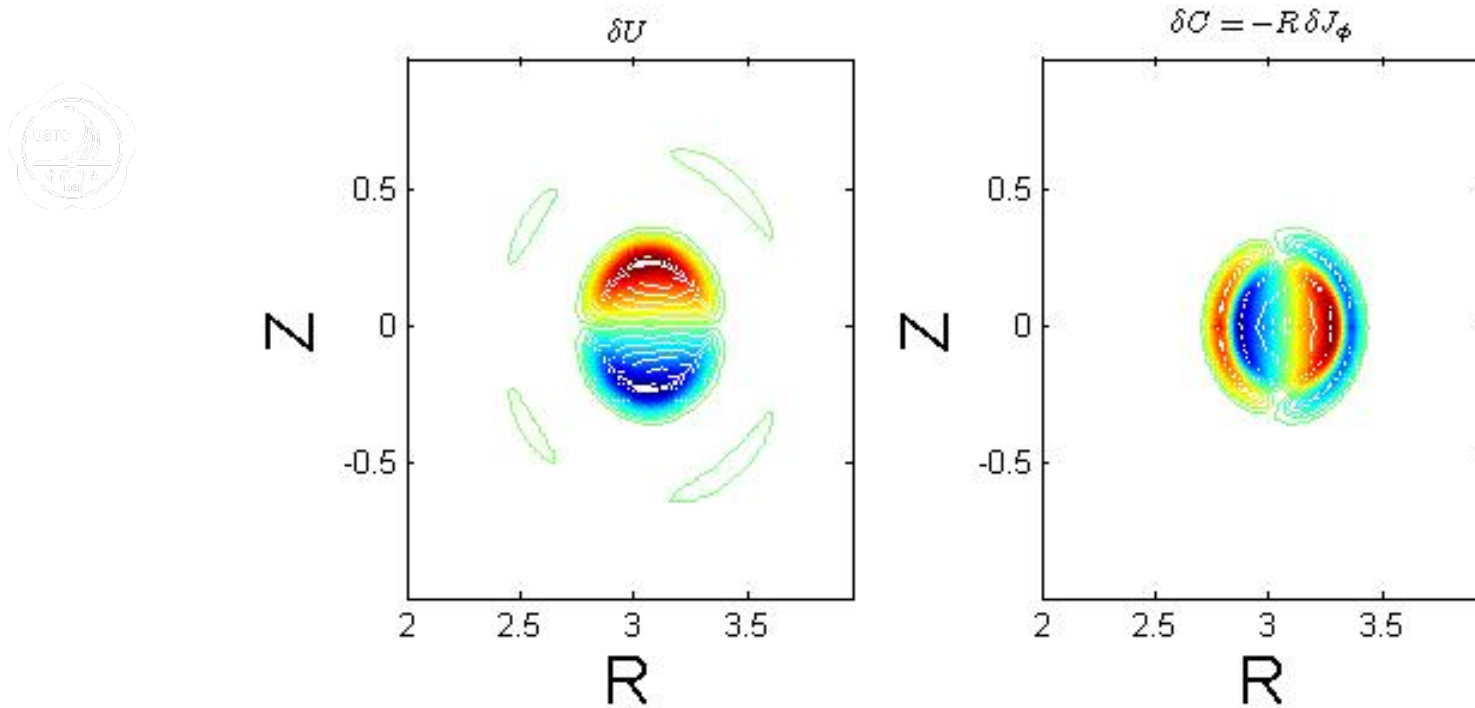
- ◆ As a first step, we consider only the effects of runaway current. The effects of runaway pressure tensor are neglected.
- ◆ For simplicity, the current is assumed to be completely carried by runaway electrons.
- ◆ Given the profile of safety factor as



- Two cases: $q_0 = 0.83, 0.93$

Linear results

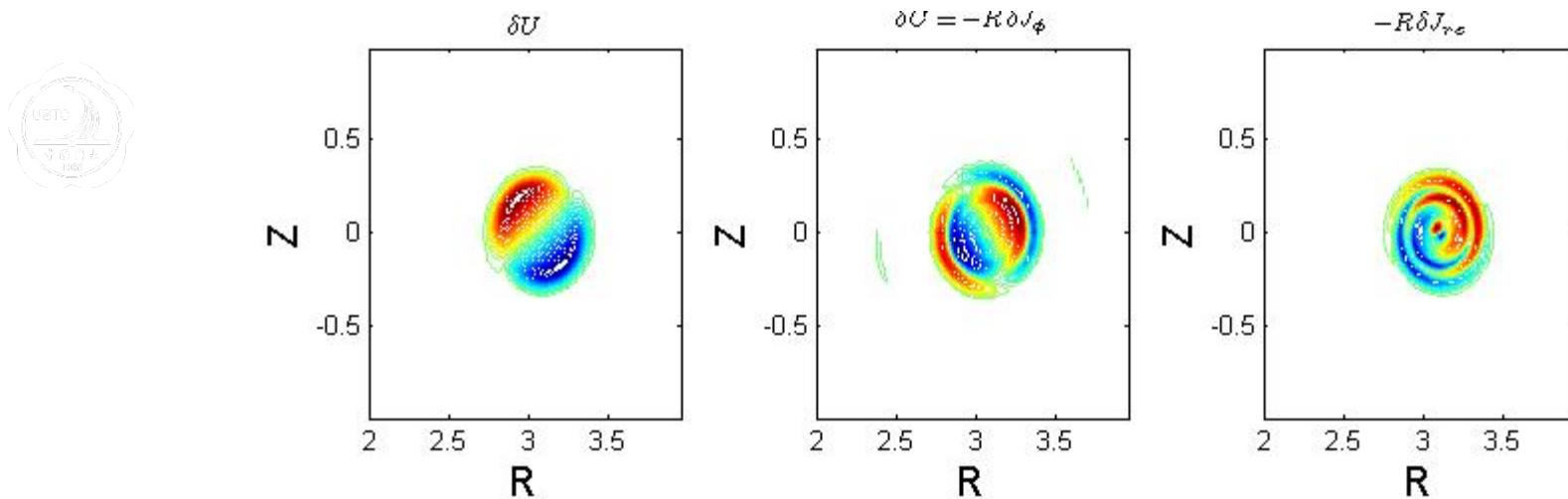
- ◆ Case1: $q_0=0.83$
- Without runaway current, the growth rate of 1/1 mode is about $2.14e-2$, the mode structures are shown below



- It is the resistive kink mode.

Linear results

- ◆ Case 1: $q_0=0.83$
- With runaway current, the growth rate of 1/1 mode is about $2.56e-2$, the mode structures are shown below



- The growth rate is enhanced slightly, and the mode structures keep almost the same.

Linear results

- ◆ The physics: the linearized equations in cylindrical geometry are

$$-(im/q - in)\delta\hat{\phi} + \gamma\delta\psi = \hat{\eta}(\nabla_{\perp}^2\delta\psi - R\delta\hat{J}_R), \quad (7)$$

$$\gamma\nabla_{\perp}^2\delta\hat{\phi} = -\frac{imR}{r}\frac{d\hat{J}_{//0}}{dr}\delta\psi + \frac{in}{q}\left(\frac{m}{n} - q\right)\nabla_{\perp}^2\delta\psi, \quad (8)$$

$$(m/q - n)\delta J_R - \frac{m}{r}\frac{d\hat{J}_R}{dr}\delta\psi = 0, \quad (9)$$

where runaway current is a flux function approximately, due to $|v_{//}| \sim c$.

Order analysis: $\delta J_{//} \sim O(\delta\psi / w_l^2)$, $\delta J_R \sim O(\delta\psi / w_l) \rightarrow \delta J_{//} > \delta J_R$

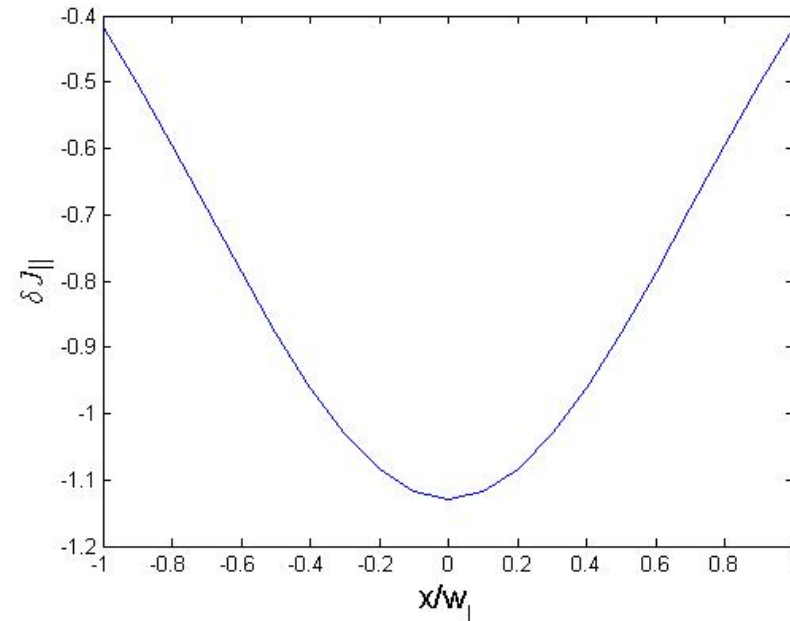
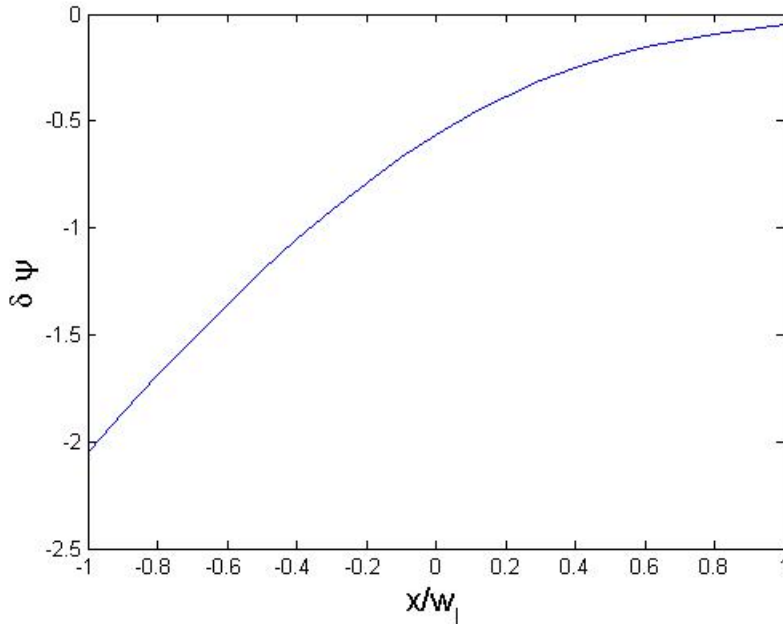
The perturbation of runaway current is of higher order.

The characteristic functions in the resistive layer without runaway are

$$\delta\psi = b/2 \left[x \operatorname{erfc}(x/w_l) - (w_l/\sqrt{\pi}) \exp(-(x/w_l)^2) \right]$$

$$\delta\phi = i(b/2) \left(w_l/\sqrt{2} \right) \operatorname{erfc}(x/w_l)$$

Linear results

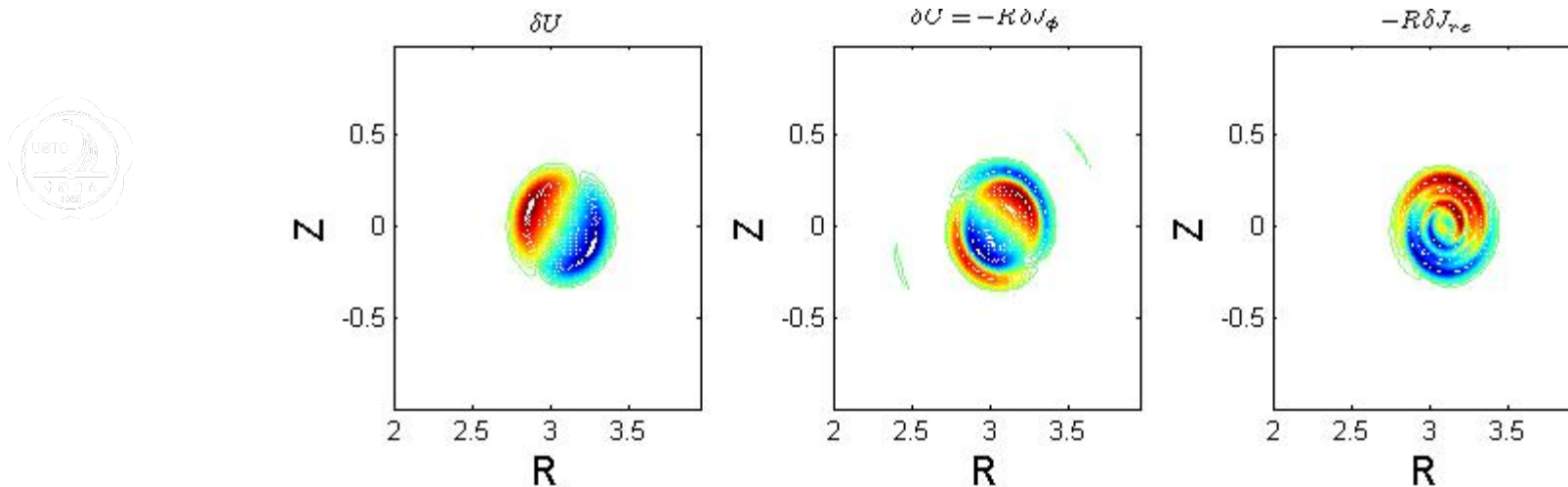


$$\delta J_R = -\frac{q_s}{s} \frac{d\hat{J}_R}{dr} \frac{\delta\psi}{x}, \quad \frac{d\hat{J}_R}{dr} < 0, \quad \Rightarrow \quad \langle \delta J_{ohm} \rangle = \langle \delta J_{||} - \delta J_R \rangle > \delta J_{||}$$

The perturbation of runaway current tends to enhance the perturbation of Ohm' current, so that it will increase the growth rate of the resistive kink mode.

Linear results

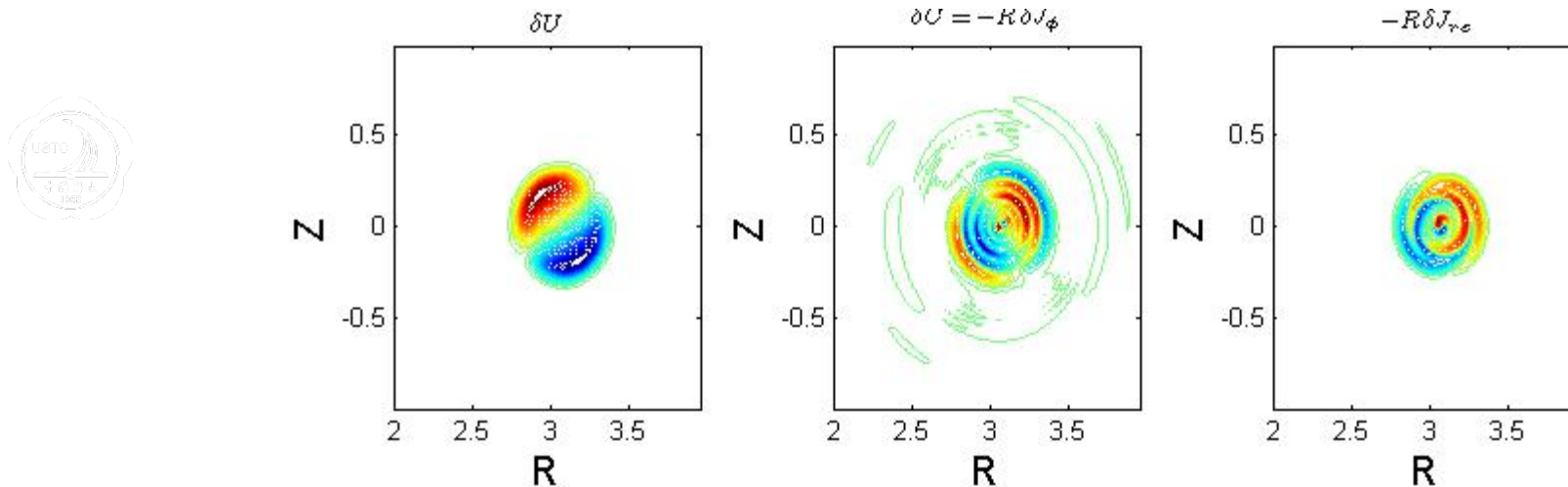
- With runaway current, without electric drift contribution in runaway equation, the growth rate is $2.45e-2$, mode structures are



- The contribution of electric drift in runaway equation is small, due to $c/v_A \gg 1$.

Linear results

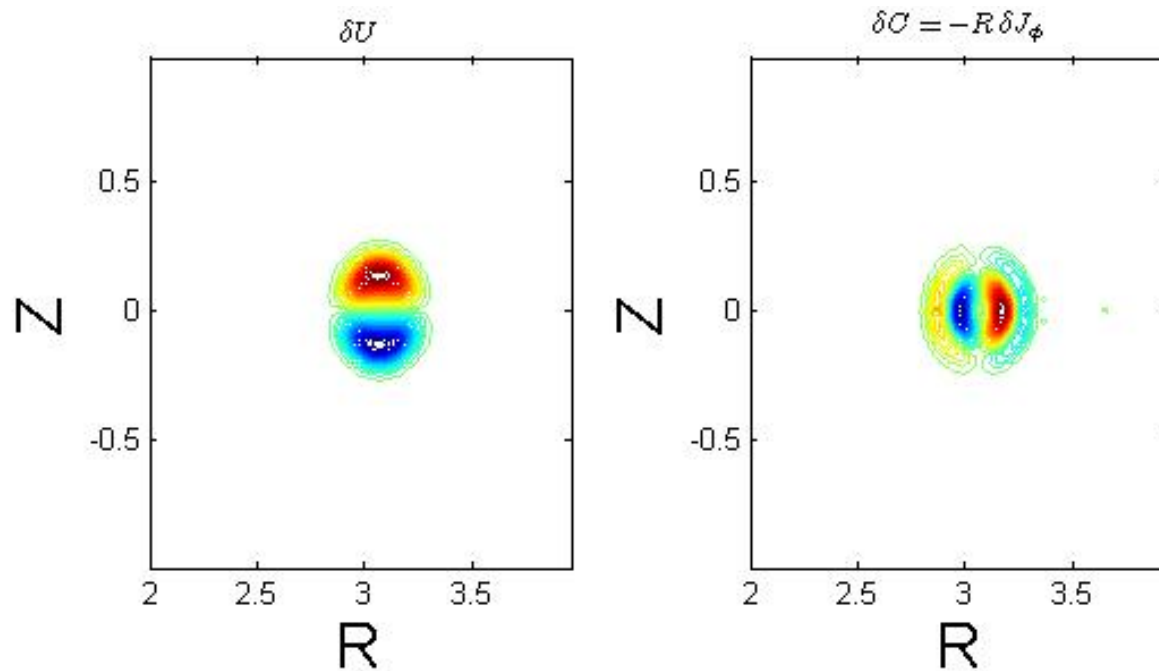
- With runaway current, without magnetic drift contribution in runaway equation, the growth rate is $2.6e-2$, mode structures are



- The effect of magnetic drift velocity is small due to $\Delta_b / \Delta_{layer} \gg 1$.

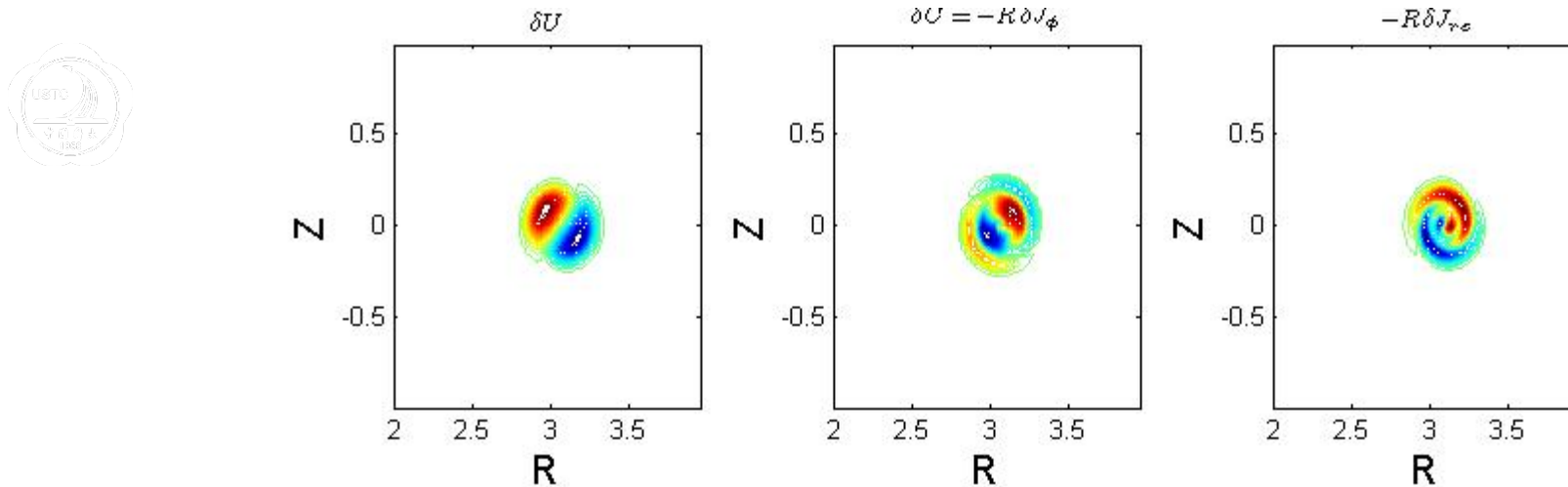
Linear results

- ◆ Case2: $q_0=0.93$
- Without runaway current, the growth rate of 1/1 mode is about $9.3e-3$, the mode structures are



Linear results

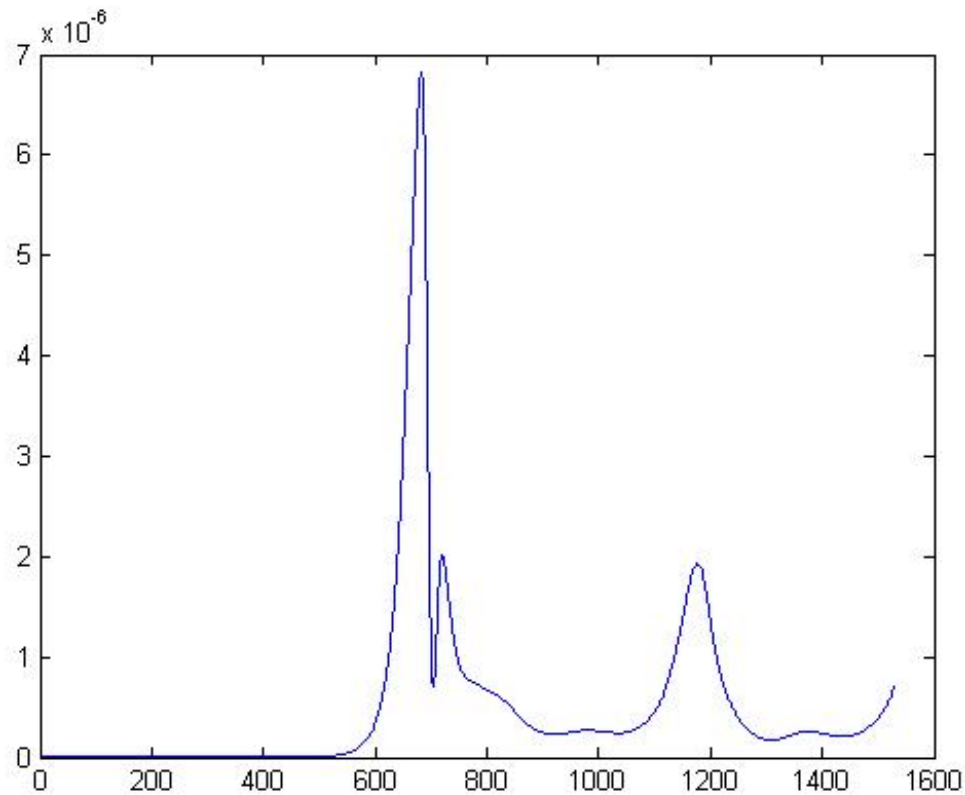
- ◆ Case 2: $q_0=0.93$
- With runaway current, the growth rate of 1/1 mode is about $1.72e-2$, the mode structures are



- The growth rate is enhanced, and the mode structures keep almost the same.

Nonlinear results

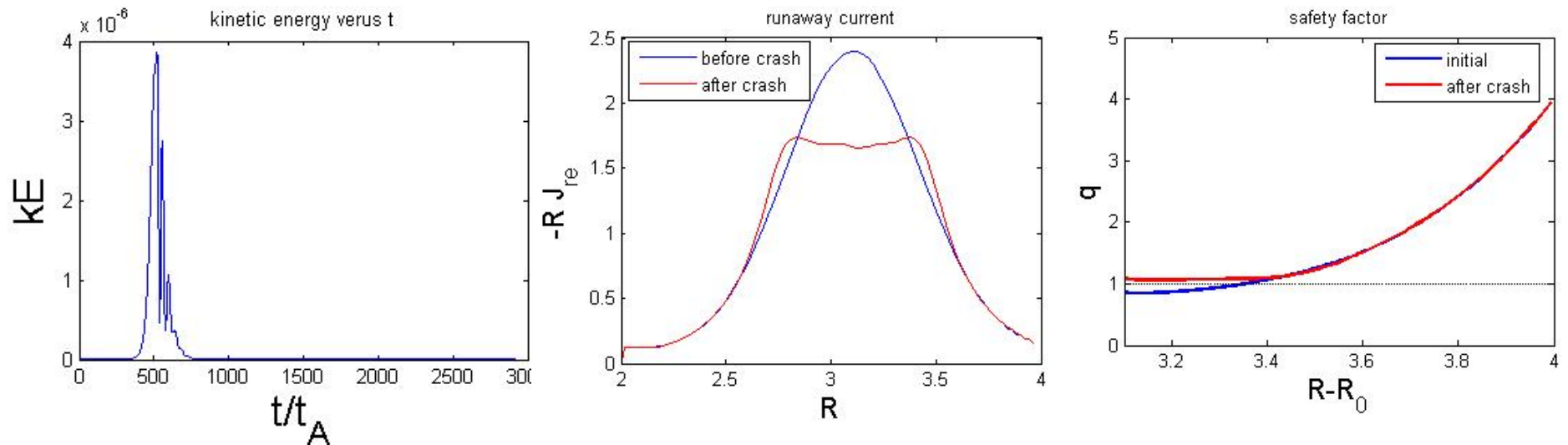
◆ Case 1: $q_0=0.83$, without runaway current



◆ The usual sawteeth are observed in the simulation.

Nonlinear results

◆ Case 1: $q_0=0.83$, with runaway current

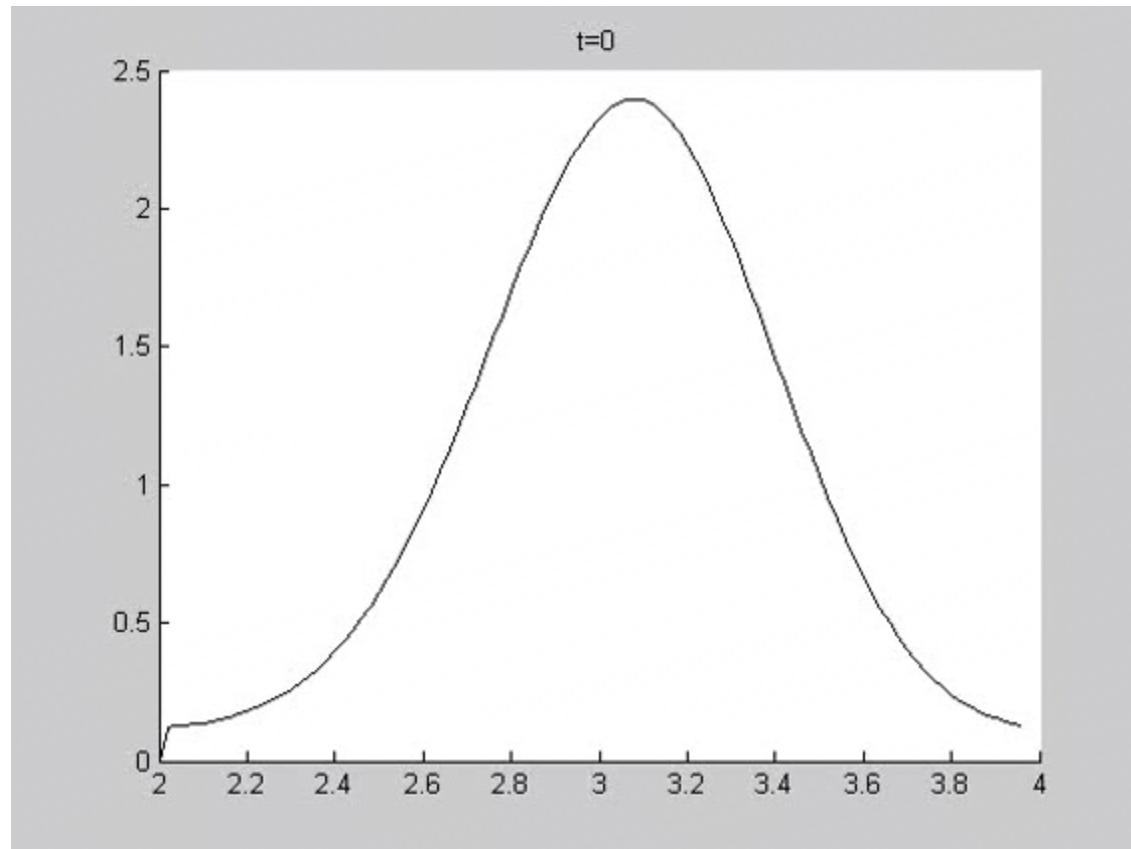


- ◆ Resistive kink mode results a single sawtooth crash only.
- ◆ A steady state with axi-symmetric equilibrium is reached after the crash.
- ◆ The plasma current and runaway current become flatten within $q=1$ surface, q_0 greater than 1.

Physics: sawtooth crash tends to flatten current within $q=1$ surface. After the crash, the runaway current, acting as a current source, stays flatten.

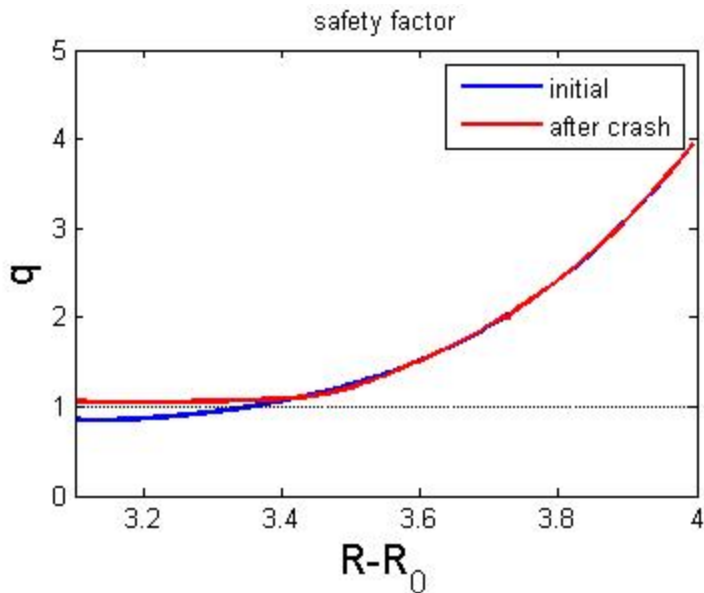
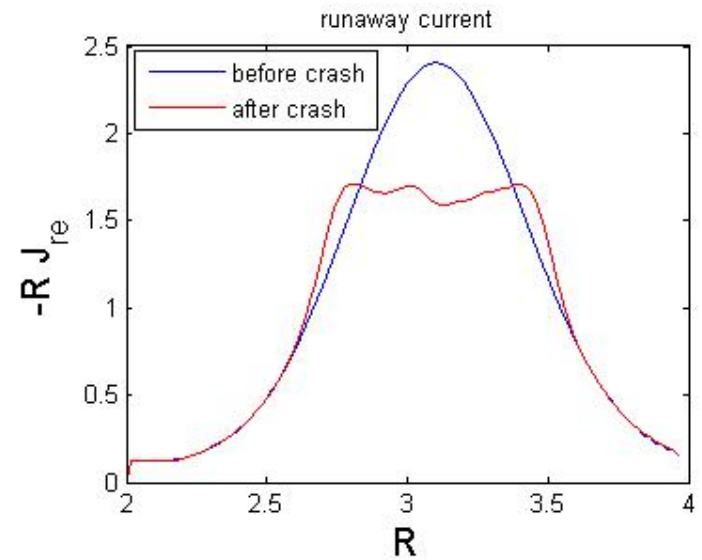
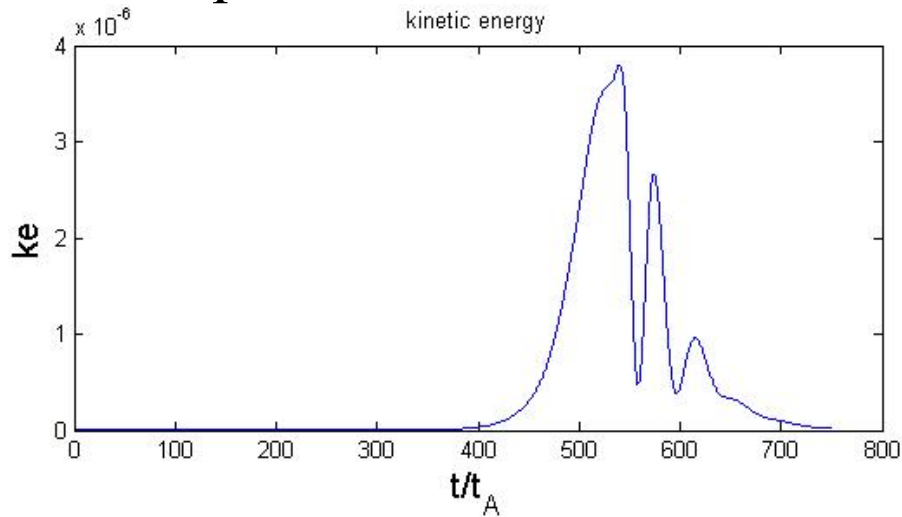
Simulation results

- The evolution of current



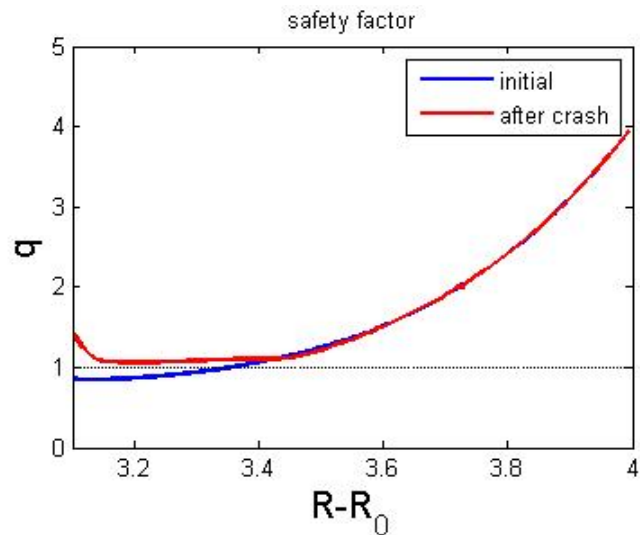
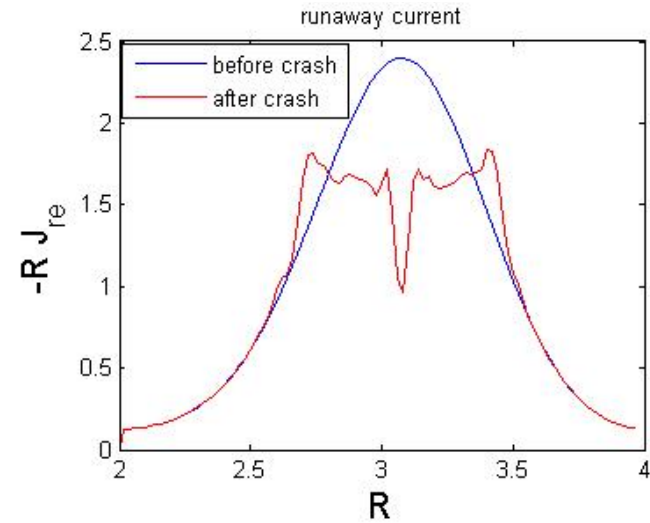
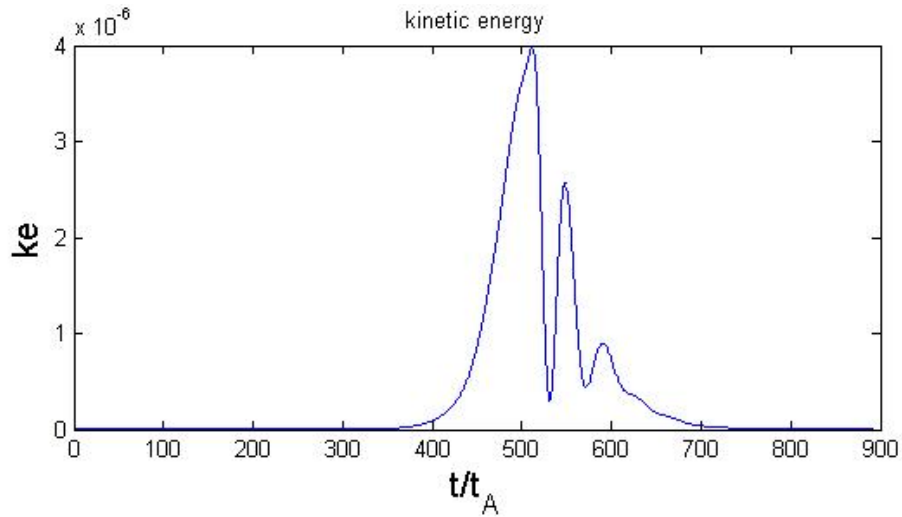
Nonlinear results

◆ Case 1: $q_0=0.83$, without electric drift,



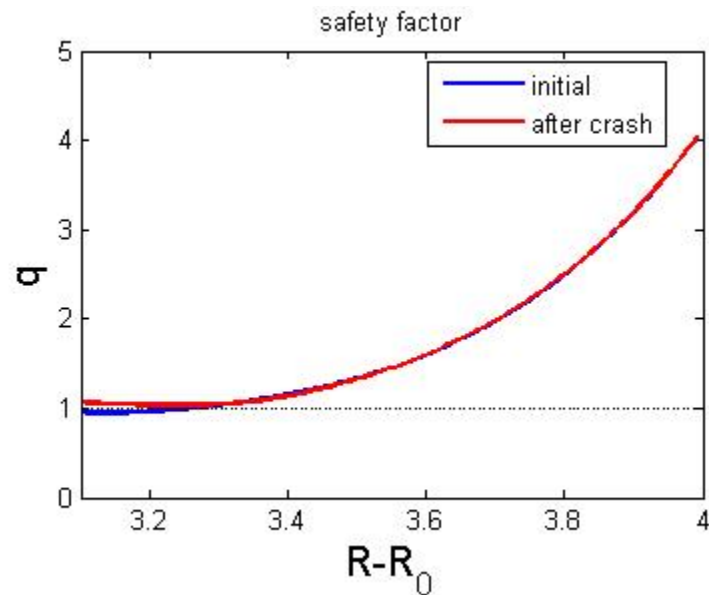
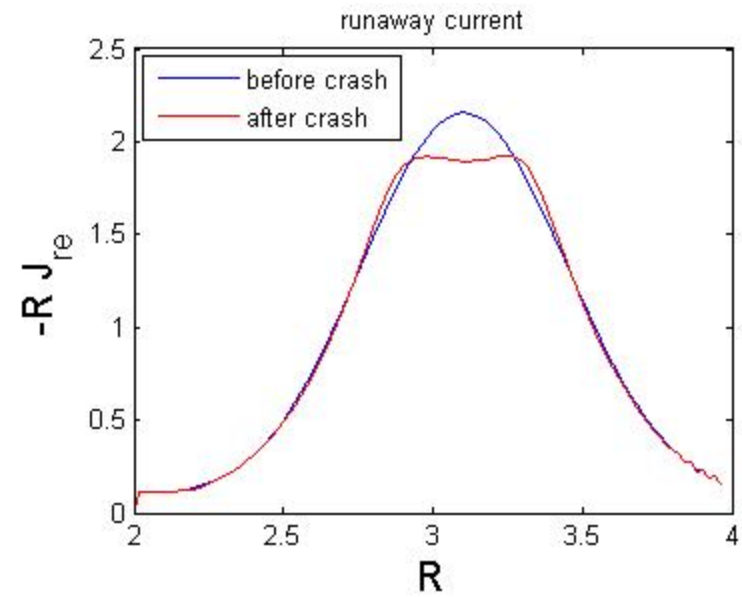
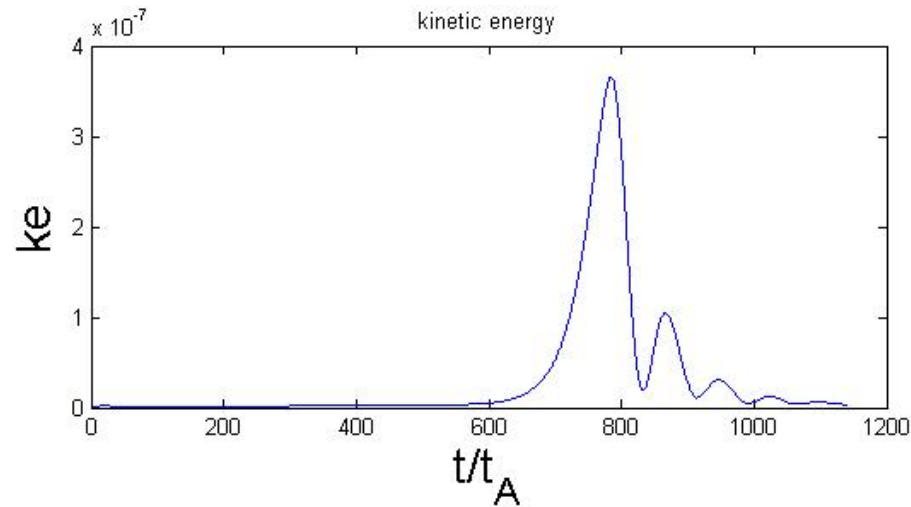
Nonlinear results

◆ Case 1: $q_0=0.83$, without magnetic drift



Nonlinear results

◆ Case2: $q_0=0.93$.



➤ The same trend with $q_0=0.83$.

Conclusion and discussion

- ◆ The linear growth rate of 1/1 resistive kink mode is enhanced by the effects of runaway current.
- ◆ After a single sawtooth crash, plasma reaches a new steady state with axi-symmetric equilibrium.
- ◆ The profiles of plasma current and runaway current are flattened within $q=1$ surface.





Thank you for your
attention!